

Temperature distribution in selective laser-tissue interaction

Jared J. Crochet

University of Central Oklahoma
Department of Physics and Engineering
Biomedical Engineering Program
100 North University Drive
Edmond, Oklahoma 73034

Surya C. Gnyawali

University of Central Oklahoma
Department of Physics and Engineering
Biomedical Engineering Program
100 North University Drive
Edmond, Oklahoma 73034
and
Oklahoma State University
Department of Physics
Stillwater, Oklahoma 74078

Yichao Chen

Evan C. Lemley

University of Central Oklahoma
Department of Physics and Engineering
Biomedical Engineering Program
100 North University Drive
Edmond, Oklahoma 73034

Lihong V. Wang

Texas A&M University
Department of Biomedical Engineering
Optical Imaging Laboratory
3120 TAMU
College Station, Texas 77843-3120

Wei R. Chen

University of Central Oklahoma
Department of Physics and Engineering
Biomedical Engineering Program
100 North University Drive
Edmond, Oklahoma 73034
E-mail: wchen@ucok.edu

1 Introduction

Laser is an effective tool in clinical applications. A particular use of laser energy is the selective photothermal interaction in cancer treatment. It has been shown that the combination of an 805-nm laser and *in situ* indocyanine green (ICG), a dye with an absorption peak around 800 nm, can result in selective heating when treating tumors buried in normal tissue.¹⁻³ Recent studies using nanoparticles as *in situ* dye also showed the selective photothermal effect.⁴ Since tumor tissue is more sensitive to temperature elevation than normal tissue,^{5,6} the control of temperature in the target region during laser irra-

Abstract. Selective photothermal interaction using dye enhancement has proven to be effective in minimizing surrounding tissue damage and delivering energy to target tissue. During laser irradiation, the process of photon absorption and thermal energy diffusion in the target tissue and its surrounding tissue are crucial. Such information allows the selection of proper operating parameters such as dye concentrations, laser power, and exposure time for optimal therapeutic effect. Combining the Monte Carlo method for energy absorption and the finite difference method for heat diffusion, the temperature distributions in target tissue and surrounding tissue in dye enhanced laser photothermal interaction are obtained. Different tissue configurations and dye enhancement are used in the simulation, and different incident beam sizes are also used to determine optimum beam sizes for various tissue configurations. Our results show that the algorithm developed in this study could predict the thermal outcome of laser irradiation. Our simulation indicates that with appropriate absorption enhancement of the target tissue, the temperature in the target tissue and in the surrounding tissue can be effectively controlled. This method can be used for optimization of lesion treatment using laser photothermal interactions. It may also provide guidance for laser immunotherapy in cancer treatment, since the immunological responses are believed to be related to tissue temperature changes. © 2006 Society of Photo-Optical Instrumentation Engineers. [DOI: 10.1117/1.2204615]

Keywords: Monte Carlo simulation; dye enhancement; photon absorption; optimal therapeutic effect; gel phantom; thermal energy diffusion; selective photothermal therapy.

Paper 05345R received Nov. 21, 2005; revised manuscript received Feb. 6, 2006; accepted for publication Feb. 6, 2006; published online May 11, 2006.

diation is crucial to the outcomes of the treatment.

Selective photothermal interaction can destroy tumor cells directly by raising the temperature of the target tissue. It can also serve as a precursor for immune activation by exposing tumor antigens, when combined with an immunotherapy-oriented treatment.^{7,8} Tumor tissue responds to thermal treatment according to the treatment conditions. High-level thermal irradiation with extra-high temperature elevation can lead to total tissue destruction with denatured cells, which do not have much effect on the host immune stimulations. Low-level thermal irradiation may not destroy enough tumor cells and/or may not expose enough tumor antigens. The optical outcome of laser photothermal interaction is to kill as much target tu-

Address all correspondence to Wei Chen, Physics and Engineering, Univ. of Central Oklahoma, 221 G Howell Hall, Edmond, Oklahoma 73034; Tel: 405-974-5198; Fax: 405-974-3812; E-mail address: wchen@ucok.edu

mor cells as possible, and at the same time preserve the tumor proteins for the immunological stimulations. Such outcome depends on the temperature distribution in the tumor tissue.

The desired thermal effect strongly depends on the laser parameters, and the tissue optical and thermal properties. In the case of dye-enhanced laser therapy, the dye administration also becomes crucial. The concentrations of the absorbing dye in, and the optical and thermal properties of, a specific target region are important factors. Improper dye administration causes undesired tissue damages or insufficient heating of target tissue. To choose the treatment parameters properly and to predict the outcome of the photothermal effect, a reliable tissue model and simulation method is needed. Since biological tissue is a turbid medium and the mean free path of the light involved in irradiation is far less than the dimension of the medium, light propagation in tissue quickly becomes a random process. The ideal mathematical tool for such a process is the Monte Carlo method.⁹⁻¹¹ The Monte Carlo method can effectively simulate absorption and scattering of the light in tissue, hence providing the spatial distribution of photon absorption. Heat transfer in the tissue during laser irradiation also affects the temperature distribution and tissue responses in the target tissue and surrounding tissue. Due to the relatively large physical dimensions and inhomogeneous characteristics of biological tissues, the diffusion process also needs to be modeled during laser irradiation. Using the absorbed energy in tissue as the heat source, the thermal energy diffusion process can be determined, hence providing information on thermal responses of tissue. In this study, Monte Carlo simulation was used to acquire the information of laser absorption in tissue, and the finite difference method for thermal diffusion in the tissue was used to determine the temperature distribution during and after laser irradiation. The dynamic processes of tissue thermal responses to laser irradiation under different tissue configurations and laser parameters are reported.

2 Monte Carlo Method for Laser-Tissue Interaction

Biological tissue is considered as a linear isotropic homogeneous medium. When a photon enters the tissue, the Monte Carlo method samples random propagation variables from a well-defined probability distribution. Selection of the step size of the photon traveling inside the tissue between two interaction sites is based on the photon's mean free path. For a specific type of tissue with an absorption coefficient μ_a and scattering coefficient μ_s , the step size is given as⁹⁻¹¹

$$s = \frac{-\ln(\zeta)}{\mu_t}, \quad (1)$$

where ζ is a random number and $\mu_t = \mu_a + \mu_s$ is the interaction coefficient.

When a photon moves from one site to the next, it will have a deflection from its original direction. We define the deflection with an angle θ and an azimuthal angle φ . The probability distribution of $\cos \theta$ is described by the scattering function:

$$p(\cos \theta) = \frac{1 - g^2}{2(1 + g^2 - 2g \cos \theta)^{3/2}}, \quad (2)$$

which was used for galactic scattering.¹² The anisotropy factor g is the average value of $\cos \theta$.

For each random step, the deflection angle is determined using the distribution in Eq. (2):

$$\cos \theta = \begin{cases} \frac{1}{2g} \left[1 + g^2 - \left(\frac{1 - g^2}{1 - g + 2g\zeta} \right)^2 \right] & \text{if } g > 0 \\ 2\zeta - 1 & \text{if } g < 0 \end{cases}. \quad (3)$$

The azimuth angle is uniformly distributed throughout the interval from 0 to 2π .

An incoming photon may hit the layer boundary when it propagates. When a photon reaches an interface, the remaining photon step is changed to $s_0 - s_1$, where s_0 is the step size at the original layer and s_1 is defined as follows:^{9,11}

$$s_1 = \begin{cases} (z - z_0)/(-\mu_z) & \text{if } \mu_z < 0 \\ (z_1 - z)/\mu_z & \text{if } \mu_z > 0 \end{cases}, \quad (4)$$

where z_0 and z_1 are the z coordinates of the upper and lower boundaries of the current layer, and μ_z is the directional cosine in the z axis.

If the photon bounces back, the photon would travel in the same layer with the same property; if the photon goes into another layer, the step size will be changed to $s' = s_0 \mu_{t0} / \mu_{t1}$, where μ_{t1} and μ_{t0} are the interaction coefficients for the new layer and the original layer, respectively.

Snell's law and Fresnel reflectance at the boundary are used to determine if the photon is reflected back or injected into the next layer.

The simulation process is as follows. A photon is launched and reaches the top of the tissue. It propagates a certain step size s , with a rotation angle φ , and deflection angle θ , to an interaction site and deposits a portion of its energy to the site, determined by the tissue optical properties. The deposition of energy is determined by the weight W that a photon leaves behind after an interaction at a specific site. The change of weight is defined as $\Delta W = W \mu_a / \mu_t$. When this value is below a desired threshold, the photon is terminated. For this simulation, we terminated a photon if one ten thousandth of its original weight was left after its interactions with the surrounding media. After termination, a new photon is launched and the process is repeated.

Once the Monte Carlo simulation is complete for all the photons, an absorption power density matrix is generated for a given tissue configuration. This matrix represents the amount of laser power absorbed by the region in the form of power density. In a cylindrical system, the absorption power density matrix is a function of the coordinates r and z , with a cylindrical symmetry. Multiplying the absorption photon probability density by the desired laser power, the total power absorbed in the region is obtained. The absorbed power at each location can be used as the heat source for the thermal diffusion process.

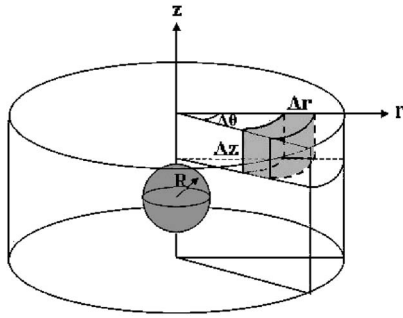


Fig. 1 Cylindrical tissue configuration for simulation. Azimuthal symmetry is assumed. The volume element is $(\Delta r)^2 \Delta z \Delta \theta / 2$, as shown in the figure. The running indices i and j for r and z , respectively, start from the top center of the cylinder ($r=0$ and $z=0$). A spherical tumor of radius R with different optical properties is shown in the center.

3 Finite Difference Method

The diffusion equation with constant thermal properties and steady heat generation can be used for laser tissue interactions,

$$\nabla^2 T(r, z, t) + \frac{\dot{q}(r, z)}{k} = \frac{\rho c}{k} \frac{\partial T(r, z, t)}{\partial t}, \quad (5)$$

where \dot{q} is the rate of heat generation inside the region (the energy density per unit time), T is the temperature, k is the thermal conductivity of the tissue, ρ is the density, and c is the specific heat. Constant thermal properties are assumed, because in most cases, temperature increase is not significant enough to change the properties of tissue. The heat generation rate is calculated as,

$$\dot{q} = \text{photon absorption probability} * \text{laser power}, \quad (6)$$

where the photon absorption probability is the portion of photon energy deposited in a unit volume, obtained by the Monte Carlo simulation.

From Eq. (6) one can find the temperature increase as a function of position and time. Using the Laplace equation in cylindrical coordinates and assuming azimuthal symmetry, Eq. (5) becomes

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T}{\partial r} \right) + \frac{\partial^2 T}{\partial z^2} + \frac{q}{k} = \frac{\rho c}{k} \frac{\partial T}{\partial t}. \quad (7)$$

This equation can be solved for an approximate temperature distribution by using forward Euler time integration, which is an explicit finite difference technique.^{13–15} Specifically, Eq. (7) can be rewritten as,

$$\frac{T_{i-1,j}^n - 2T_{i,j}^n + T_{i+1,j}^n}{(\Delta r)^2} + \frac{1}{i\Delta r} \frac{T_{i+1,j}^n - T_{i-1,j}^n}{2\Delta r} + \frac{T_{i,j-1}^n - 2T_{i,j}^n + T_{i,j+1}^n}{(\Delta z)^2} + \frac{q_{i,j}^n}{k} = \frac{\rho c}{k} \frac{T_{i,j}^{n+1} - T_{i,j}^n}{\Delta t}, \quad (8)$$

where $T_{i,j}$ is the temperature matrix [(i, j) represents a volume element as shown in Fig. 1], obtained using appropriate initial conditions, boundary conditions, and heat generation rate

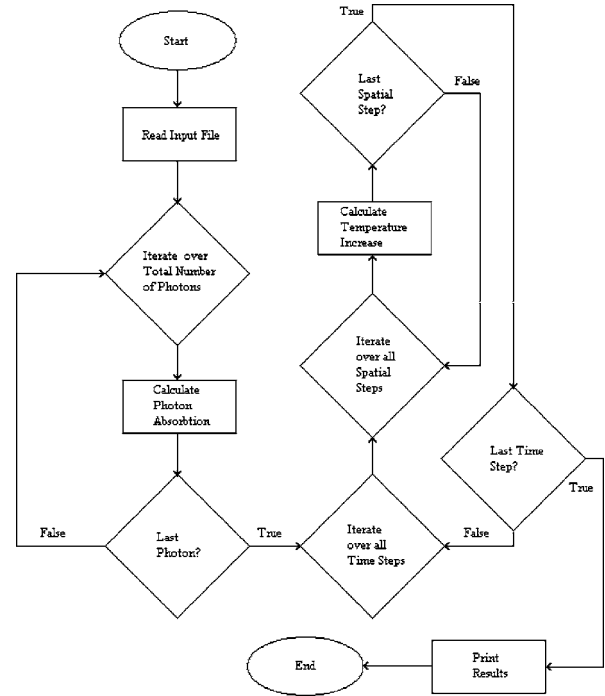


Fig. 2 Flow chart of the simulations for photon absorption and heat diffusion. The Monte Carlo simulation for the energy deposition is performed first until every photon has propagated through the media. After the absorption power density matrix is determined, the finite difference method starts to determine the heat diffusion and temperature distribution.

\dot{q} .^{13–15} For the solution to converge and be stable, the time step is limited to

$$\Delta t \leq \frac{1}{4} \frac{(\Delta r)^2}{\alpha}, \quad (9)$$

where $\alpha = k/\rho c$. This value corresponds to a mesh Fourier number $F_{0m} \equiv \alpha \Delta t / (\Delta r)^2 \leq 1/4$. Values above 1/4 will cause the average temperature at location (i, j) to overshoot the average of its nearest neighbors.^{13–15}

The boundaries of the cylinder are subjected to convection, which follows a Neumann boundary condition. The convection condition at the top of the cylinder is given by,

$$-k \frac{\partial T}{\partial z} = h(T_b - T_\infty), \quad (10)$$

where h is the convection constant, and T_b and T_∞ are the temperatures of the boundary and the environment, respectively. Similarly, at the bottom of the cylinder the same condition applies, but there is a sign change on the derivative due to the orientation of the coordinate system. The outer surface of the cylinder is also subjected to convection, and the heat transfer can be treated similarly.

The center of the cylinder must be treated with care, since the Laplacian is singular at the origin. Symmetry can be used to avoid the singularity. Specifically, as r approaches zero following a radial path, the slope of the temperature field vanishes,

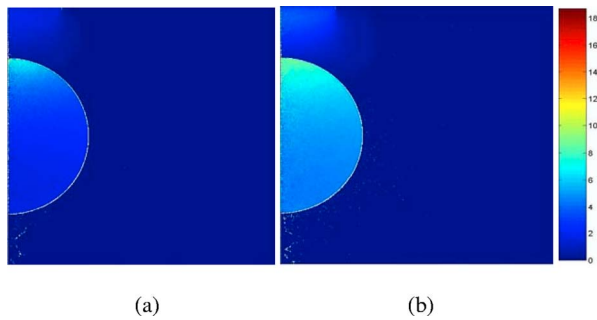


Fig. 3 Photon absorption power density matrix of a cylindrical tissue of 1-cm radius and 1-cm height, with a dye-enhanced spherical tumor of 0.3-cm radius buried 0.2 cm below the surface. A total of 100,000 photons was used and the beam radius is 0.2 cm. Because of the cylindrical symmetry, only half of the tissue-tumor configuration is shown. Tumor absorption coefficients are (a) 0.2 cm⁻¹ and (b), 0.6 cm⁻¹. The surrounding tissue in both cases has an absorption coefficient of 0.1 cm⁻¹. All other optical properties are the same (see Tables 1 to 4). The scale is the probability density 10⁻³ × 1/cm³.

$$\left. \frac{\partial T}{\partial r} \right|_{r=0} = 0. \quad (11)$$

The approximated value of this boundary can be found by

$$\frac{1}{r} \frac{\partial T}{\partial r} \approx \frac{\partial^2 T}{\partial r^2}. \quad (12)$$

This can be validated by the fact that at the origin, the temperature from $i=-1$ to $i=1$ can be approximated to be the same. Therefore, the slope of the temperature distribution across the center of the cylinder vanishes, allowing the second derivative to vanish also. This condition requires $T_{i+1,j} = T_{i-1,j}$. With boundary conditions, all the nodes can be obtained by iterating over all of the individual space steps dictated by the physical size of the region to be simulated. Also, one should notice that Eq. (8) can be used for all space steps, but at the boundaries the appropriate substitutions must be made as dictated by the boundary conditions.

4 Simulations of Energy Distribution and Thermal Diffusion

The coordinate system of the simulation is a cylinder with user-defined radius and height. For simplicity, the radius and

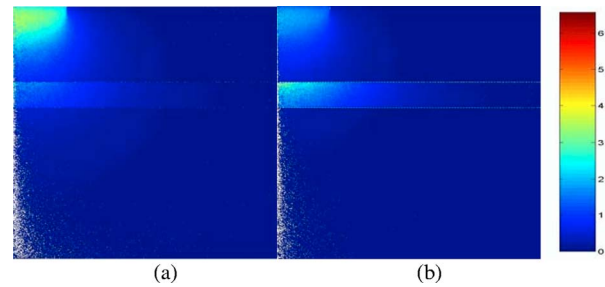


Fig. 4 Photon absorption power density matrix of a cylindrical tissue of 1-cm radius and 1-cm height, with a dye-enhanced flat tissue layer of 0.1-cm thickness, buried 0.3 cm below the surface. A total of 100,000 photons was used and the beam radius is 0.2 cm. Because of the cylindrical symmetry, only half of the configuration is shown. The absorption coefficients of the buried layer are (a) 0.2 cm⁻¹ and (b) 0.6 cm⁻¹. The surrounding tissue in both cases has an absorption coefficient of 0.1 cm⁻¹. All other optical properties are the same (see Tables 1 to 4). The scale is the probability density 10⁻³ × 1/cm³.

the height were chosen to be the same in our study. The cylinder configuration may consist of different layers with varying optical and thermal properties, or with an embedded spherical tumor, as shown in Fig. 1. Using the method described in Sec. 2, algorithms are constructed to determine the energy deposition using Monte Carlo simulation. Then, the finite difference method is used for the determination of heat and temperature distribution. Figure 2 shows the flow of the simulation process. The beam properties must be taken into consideration, since it is the source of the energy. A flat circular beam, which can be achieved experimentally by using a fiber fitted with a diffusing lens, is usually used in laser thermal treatment. In this simulation, the flat incident beam is constructed of multiple concentric rings. Each ring consists of an equally weighted number of photons to produce an isotropic incident beam. For a desired beam radius, the number of rings may be increased to approach a continuum of incident energy. A total of 100,000 photons was used in each of the simulations in this study.

Given in Tables 1–4 are the tissue optical and thermal properties, laser beam parameters, and tissue configurations used in this simulation, based on experimentally measured values for different types of tissue,^{9,11} and on desired target tissue absorption properties.

Using the finite difference method, the temperature increase as a function of space and time are obtained by a simple explicit iterative process. The temperature simulation

Table 1 Tissue optical properties used in the simulation.

| Symbol | Physical variable | Unit | Values used in this study |
|---------|------------------------|------|---|
| μ_a | Absorption coefficient | 1/cm | 0.01 for normal tissue 1.0 for dye-enhanced tissue |
| μ_s | Scattering coefficient | 1/cm | 100 for normal tissue 100 for dye-enhanced tissue |
| n | Index of refraction | | 0 for normal tissue 1 for dye-enhanced tissue |
| g | Anisotropy | | 0.9 for normal tissue 0.9 for dye-enhanced tissue |

Table 2 Tissue thermal properties used in the simulation.

| Symbol | Physical variable | Unit | Values used in this study |
|--------|---------------------------|----------------------|---------------------------|
| ρ | Density | g/cm ³ | 1.07 |
| k | Thermal conductivity | W/cm°C | 0.0056 |
| c | Specific heat | J/g°C | 3.4 |
| h | Heat transfer coefficient | W/cm ² °C | 0.000433 |
| T_0 | Initial layer temperature | °C | 0.0 |

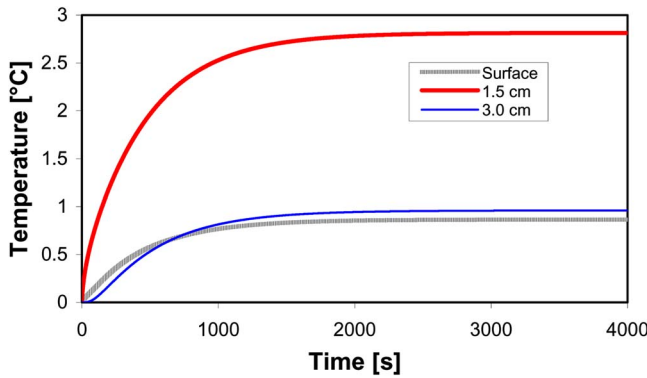


Fig. 5 Temperature at different locations during laser irradiation inside a cylinder tissue of 3-cm radius and 3-cm height, with a 0.2-cm flat layer placed in the center with an absorption coefficient of 1.0 1/cm. The laser beam has a size of 3.0-cm radius with a power of 5.0 W. Both the top and bottom of the cylinder are subjected to natural convection with $h=0.00433$ W/cm²°C. Thermal properties are $k=0.0056$ W/cm°C, $c=3.4$ J/g°C, and $\rho=1.07$ g/cm³. Irradiation time is 4000 s. The steady state is achieved at approximately 3000 s. The gray curve represents the temperature at the surface, the thick solid curve represents the temperature in the middle (1.5 cm below the surface, with dye enhancement), and the thin solid curve represents the temperature at the bottom (3 cm below the surface).

follows the photon diffusion, as described in Fig. 2. The generator of the thermal energy is the product of the absorption power density matrix obtained by the Monte Carlo function and the desired laser power. This heat generation is taken to be constant throughout the irradiation process. The energy transport is governed by the thermal properties of the region as given in Table 2, which are accepted values for biological tissue.¹³

5 Results

A cylindrical tissue of 1-cm radius and 1-cm height with a dye-enhanced spherical tumor of 0.3-cm radius was used to mimic a buried tumor in normal tissue. This system was irradiated by a laser beam of 0.2-cm radius. The photon absorption power density matrix is shown in Fig. 3 for a tumor of 0.2-cm⁻¹ absorption coefficient [Fig. 3(a)] and for a tumor of 0.6-cm⁻¹ absorption coefficient [Fig. 3(b)]. With the absorption enhancement, the buried tumor absorbed more photons than the surrounding normal tissue.

Table 3 Laser beam parameters used in the simulation.

| Symbol | Physical variable | Unit | Values used in this study |
|---------|------------------------------------|------|---------------------------|
| P | Power | W | 1.7 to 5.0 |
| br | Beam radius | cm | 0.5 to 3.0 |
| $nring$ | Number of rings within beam | | 10 to 100 |
| $nphot$ | Number of photons to be propagated | | 10 ⁵ |
| bt | Beam type (flat or Gaussian) | | |

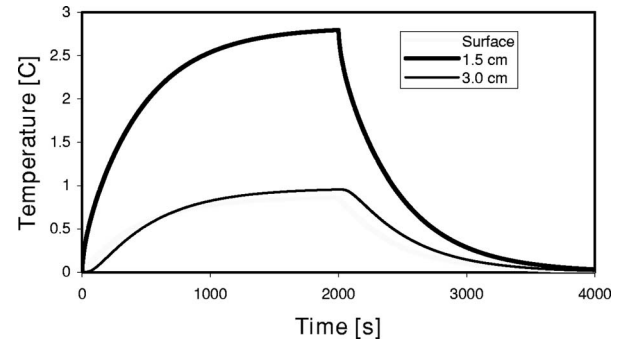


Fig. 6 Temperature at different locations during laser irradiation inside a cylinder tissue of 3-cm radius and 3-cm height, with a 0.2-cm flat layer placed in the center with an absorption coefficient of 1.0 1/cm. The laser beam has a size of 3.0-cm radius with a power of 5.0 W. Both the top and bottom of the cylinder are subjected to natural convection with $h=0.00433$ W/cm²°C. Thermal properties are $k=0.0056$ W/cm°C, $c=3.4$ J/g°C, and $\rho=1.07$ g/cm³. Irradiation time is 2000 s. The system cools to its original temperature around 4000 s. The gray curve represents the temperature at the surface, the thick solid curve represents the temperature in the middle (1.5 cm below the surface, with dye enhancement), and the thin solid curve represents the temperature at the bottom (3 cm below the surface).

The geometrical configuration is important in photon absorption. In cancer treatment, different tissue layers with different optical properties may exist in and around the target region. Figure 4 depicts the photon absorption in a configuration of normal tissue (a cylinder of radius 1 cm and height 1 cm) with a flat layer of dye-enhanced tissue (0.1-cm thickness) 0.3 cm below the surface. The selective photon absorption can be observed in this configuration.

A larger cylindrical system, 3-cm radius and 3-cm height with a flat dye-enhanced layer of 0.2-cm thickness placed in the center of the cylinder, was used for the temperature simulation. The laser beam was 3 cm in radius with 5-W power and an irradiation duration of 4000 s. The temperature

Table 4 Geometrical tissue configurations used in the simulation.

| Symbol | Physical variable | Unit | Values used in this study |
|--------|----------------------------------|------|---------------------------|
| dr | Radial space increment | cm | 0.03 |
| dz | Axial depth increment | cm | 0.03 |
| nr | Number of radial increments | | 100 |
| nz | Number of axial depth increments | | 100 |
| na | Number of angular subdivisions | | 30 |
| nl | Number of tissue layers | | 1–3 |
| hi | Top of layer | cm | |
| hf | Depth of layer | (cm) | |
| d | Depth of spherical layer | (cm) | 1.0 or 3.0 |
| r | Radius of spherical layer | (cm) | 1.0 or 3.0 |

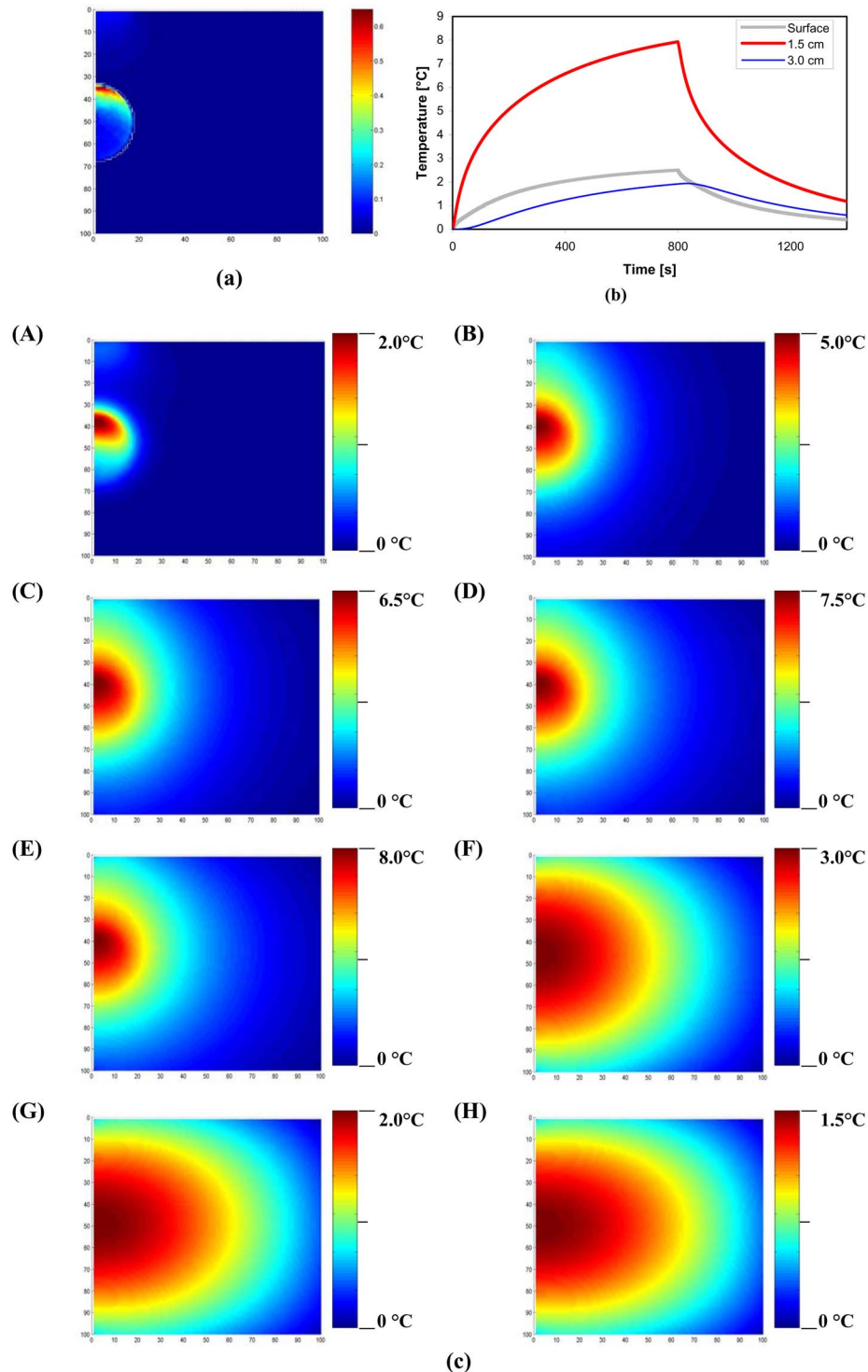


Fig. 7 (a) Photon absorption power density matrix obtained by the Monte Carlo simulation for a cylinder of 3.0-cm radius and 3.0-cm height. A tumor with a radius of 0.5 cm was placed in the center with an absorption coefficient of 1.0 $1/\text{cm}$. Due to symmetry, only half of the cylinder is shown. The cross section is through the center of the cylinder with the laser beam incident from the top. The laser beam has a 0.5-cm radius with a power of 1.7 W. The irradiation time is 800 s. The scale bar represents power absorbed by the region in W/cm^3 . (b) Temperature profiles at the center of the cylinder $T(0, z, t)$ at different depths and different time points during and after laser irradiation. The irradiation time is 800 s. Both the top and bottom of the cylinder are subjected to natural convection. The gray curve represents the temperature at the surface, the thick solid curve represents the temperature in the middle (1.5 cm below the surface, with dye enhancement), and the thin solid curve represents the temperature at the bottom (3 cm below the surface). (c) Temperature distributions at different time frames during and after laser irradiation. The cross sections are through the center of the cylinder and only half of the cylinder is shown here: (A) 10 s after laser the start of the laser irradiation, and (B) through (H) 200 to 1400 s, with a 200-s increment, after the start of the laser irradiation.

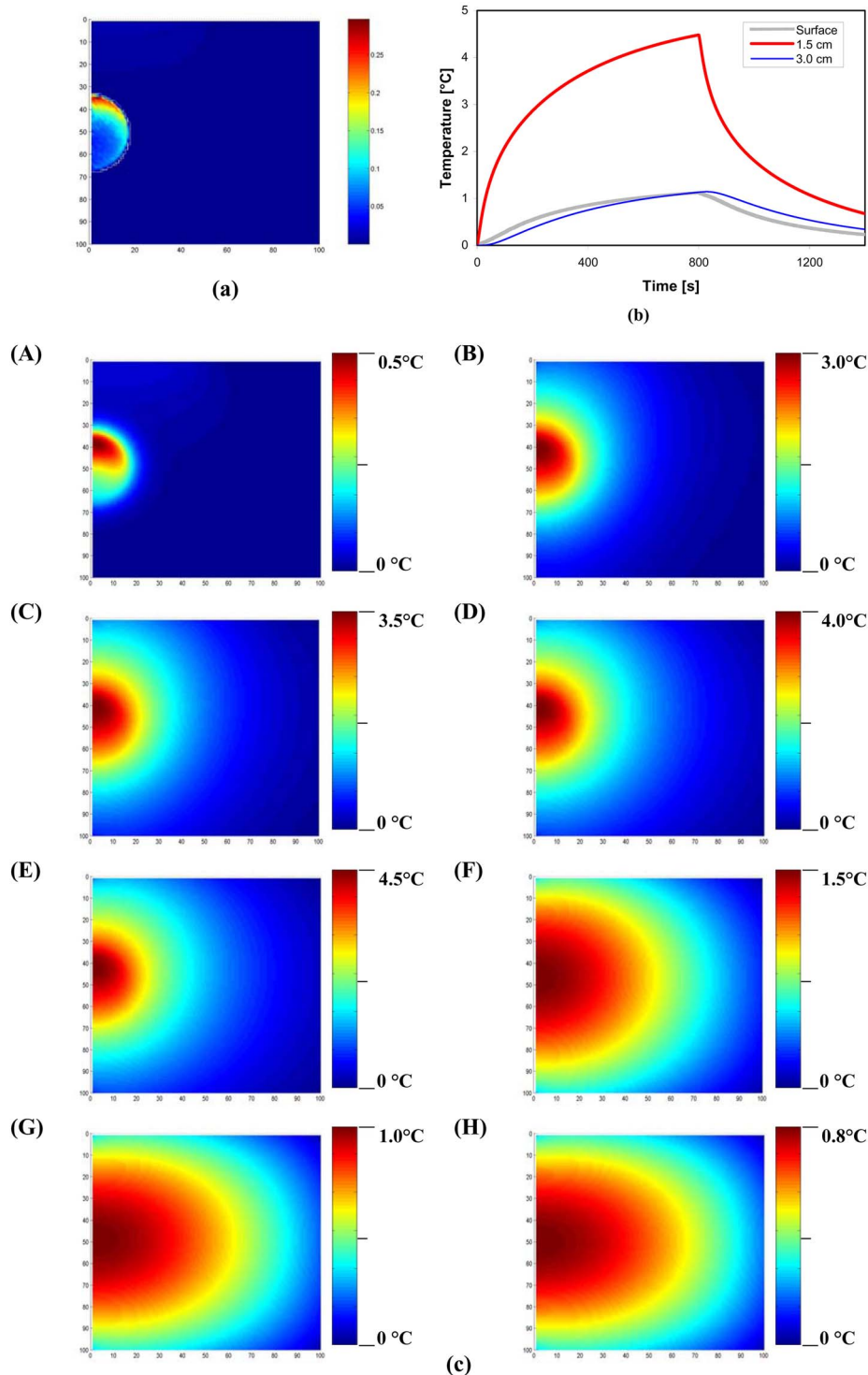


Fig. 8 (a) Photon absorption power density matrix obtained by the Monte Carlo simulation for a cylinder of 3.0-cm radius and 3.0-cm height. A tumor with a radius of 0.5 cm was placed in the center with an absorption coefficient of 1.0 1/cm. Due to symmetry, only half of the cylinder is shown. The cross section is through the center of the cylinder with the laser beam incident from the top. The laser beam has a 1.5-cm radius with a power of 1.7 W. The irradiation time is 800 s. The scale bar represents power absorbed by the region in W/cm^3 . (b) Temperature profiles at the center of the cylinder $T(0, z, t)$ at different depths and different time points during and after the laser irradiation. The irradiation time is 800 s. Both the top and bottom of the cylinder are subjected to natural convection. The gray curve represents the temperature at the surface, the thick solid curve represents the temperature in the middle (1.5 cm below the surface, with dye enhancement), and the thin solid curve represents the temperature at the bottom (3 cm below the surface). (c) Temperature distributions at different time frames during and after the laser irradiation. The cross-sections are through the center of the cylinder and only half of the cylinder is shown here: (A) 10 s after laser the start of the laser irradiation, and (B) through (H) 200 to 1400 s, with a 200-s increment, after the start of the laser irradiation.

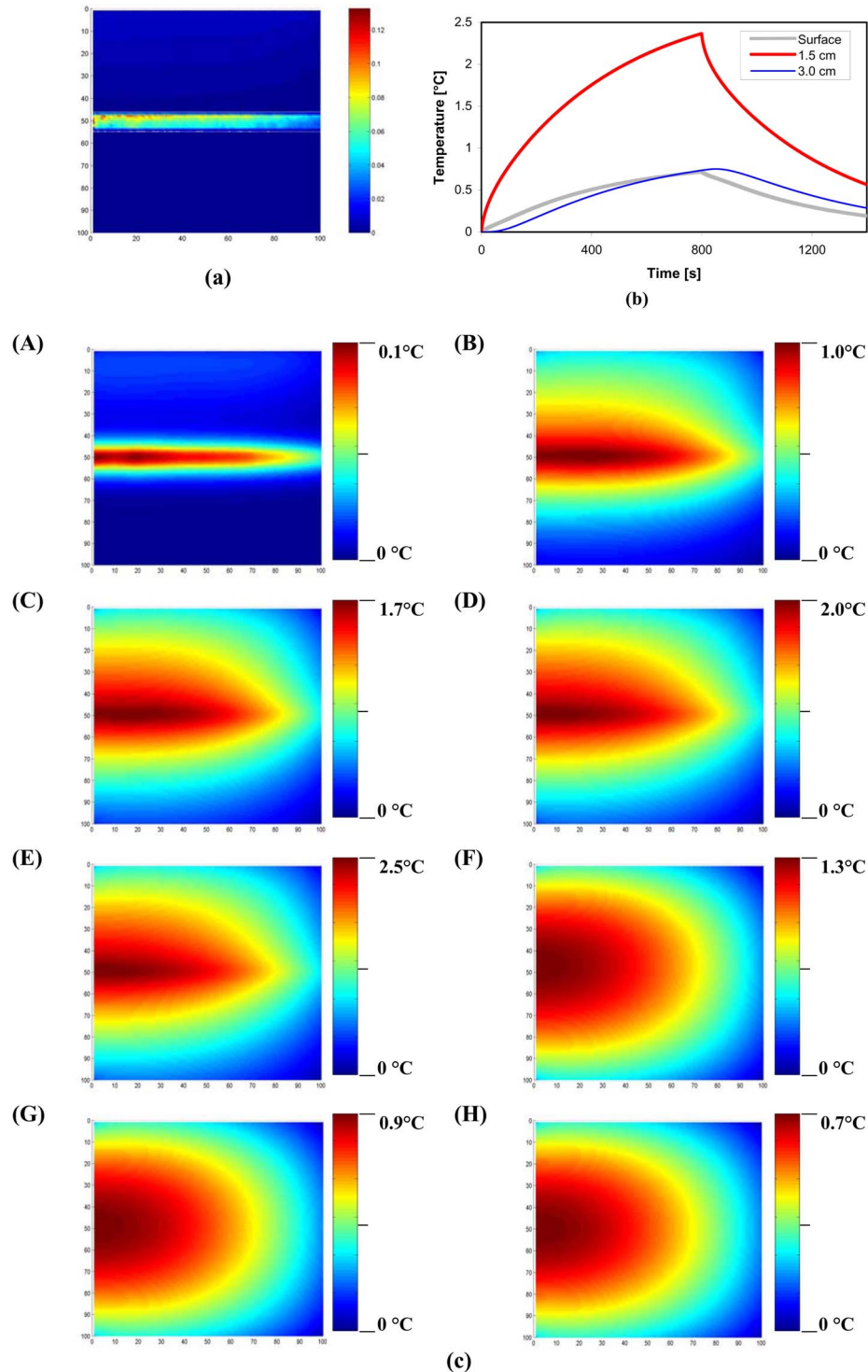


Fig. 9 (a) Photon absorption power density matrix obtained by the Monte Carlo simulation for a cylinder of 3.0-cm radius and 3.0-cm height. A 0.2-cm flat layer was placed in the center with an absorption coefficient of 1.0 $1/\text{cm}$. Due to symmetry, only half of the cylinder is shown. The cross section is through the center of the cylinder with the laser beam incident from the top. The laser beam has a 3.0-cm radius with power of 5.0 W. The scale bar represents power absorbed by the region in W/cm^3 . (b) Temperature profiles at the center of the cylinder $T(0, z, t)$ at different depths and different time points during and after the laser irradiation. The irradiation time is 800 s. Both the top and bottom of the cylinder are subjected to natural convection. The gray curve represents the temperature at the surface, the thick solid curve represents the temperature in the middle (1.5 cm below the surface, with dye enhancement), and the thin solid curve represents the temperature at the bottom (3 cm below the surface). (c) Temperature distributions at different time frames during and after laser irradiation. The cross sections are through the center of the cylinder and only half of the cylinder is shown here: (A) 10 s after laser the start of the laser irradiation, and (B) through (H) 200 to 1400 s, with a 200-s increment, after the start of the laser irradiation.

changes inside the tissue at three different locations (surface of the cylinder, the center of the dye-enhanced layer, and the bottom of the cylinder) are shown in Fig. 5. As shown in Fig. 5, the dye-enhanced layer had the most temperature increase. Figure 6 shows the temperature changes under the same conditions as those of Fig. 5, except for an irradiation duration of 2000 s, followed by 2000 s cooling time.

Different beam sizes were used to irradiate a cylindrical tissue system with a 3-cm radius and 3-cm height with a dye-enhanced tumor of 0.5-cm radius at the center. The laser power was 1.7 W. The photon absorption density matrix, the temperatures at selected locations, and the temperature distributions as function of time were obtained for a laser beam of 0.5-cm radius (Fig. 7) and of 1.5-cm radius (Fig. 8). With dye enhancement, the tumor strongly absorbs the laser energy, as shown in Figs. 7(a) and 8(a). When a smaller laser beam was used, the target temperature increase was much more significant [Fig. 7(b)] than that of a larger laser beam [Fig. 8(b)], although the thermal diffusion process for both cases followed a similar pattern as shown in Figs. 7(c) and 8(c).

Figure 9 shows the simulation results of a dye-enhanced flat layer placed at the center of a cylinder. A 0.2-cm flat layer was placed in the center with an absorption coefficient of 1.0-cm^{-1} . A 3.0-cm radius beam with power of 5.0 W was used. The photon absorption power density is given in Fig. 9(a), the temperatures at different locations are given in Fig. 9(b), and the temperature distribution at different time frames is given in Fig. 9(c). Although the laser power is high, the temperature increase is moderate due to the large laser beam.

6 Discussion

Using the Monte Carlo method and a finite difference algorithm, we studied the absorption of laser light by tissue of different optical properties, specifically for dye-enhanced target tissue buried in normal tissue. To theoretically predict the temperature increase, we designed an algorithm that calculated the temperature increase of a target tissue that was selectively heated. It takes into consideration the photon diffusion from a laser source using the Monte Carlo method and the thermal diffusion using the explicit finite difference method. The effectiveness of these methods can be easily coupled to model the entire photon/heat diffusion process.

The absorption power density matrices and the temperature distributions in different tissue configurations were obtained. The objective in laser photothermal therapy is to achieve the maximum light absorption in the target region and minimum damage to the surrounding tissue. We demonstrated the feasibility of the thermal selectivity using the simulation of a spherical target embedded within normal tissue. The absorption power density matrices shown in Figs. 3 and 4 illustrate the importance of the proper choice of absorption coefficient in selectively heating the target tissue.

The temperatures at different locations (Fig. 5) not only showed thermal selectivity in the dye-enhanced target tissue, but also showed the time course of thermal equilibrium during laser irradiation. Under the given conditions, the thermal equilibrium was reached 3000 s after the start of the laser irradiation. The thermal relaxation process was shown in Fig. 6.

Figures 7–9 vividly illustrated the dynamics of the thermal responses of tissue systems containing dye-enhanced targets

in different configurations. The impact of beam size is demonstrated in Figs. 7 and 8. Under the same laser power, a small, more concentrated laser beam apparently was more effective in raising the temperature of the target tissue (Fig. 8). An optimal combination of dye concentration, tissue configuration, and laser parameters can lead to a desired photothermal cancer treatment regimen.

When treating tumors *in vivo*, perfusion in the tumor and its surround structure will cause significant heat loss. Therefore, further studies to simulate the dye-enhanced photothermal interaction should include the heat loss term due to perfusion. In such a case, the thermal equilibrium shown in Figs. 5 and 6 will be different. However, with appropriate dye and irradiation doses, thermal equilibrium at a desired temperature can be achieved. Such a tradeoff can also be achieved by choosing the appropriate beam size. A smaller beam spot can result in a higher temperature increase, particularly in the central region of the target, as shown in Fig. 7. A wider beam with the same power can result in a much lower temperature increase in the target region, as shown in Fig. 8. This is due to the fact that the majority of the photons from the wide beam would miss the dye-enhanced target, hence reducing the overall absorption by the target. Therefore, final treatment protocol will be a function of target configuration, beam size, dye dose, and irradiation dose.

In the treatment of animal tumors, indocyanine green (ICG) has been used as the light absorbing dye for enhancement of selective photothermal interaction.^{1–3} The pharmacokinetic properties of ICG indicate a rapid hepatic excretion, and the differential uptake of ICG by tumor cells is not as significant as certain photosensitizers. Therefore, a systemic administration of ICG is not realistic for the proposed selective photothermal interaction for tumor destruction through prolonged laser irradiation. That is the reason why intratumoral administration of ICG has been adopted for tumor treatment and the desired selective photothermal effects have been observed.^{1–3}

The main goal of laser cancer treatment is to selectively destroy the cancer cells without denaturing the proteins. This allows the body's immune system to recognize the tumor as "foreign" and to mount a systemic attack on the tumors. This goal can be achieved by a carefully designed treatment protocol with optimal operating parameters. The results obtained in this study demonstrate the feasibility of such a treatment regimen and the method developed in this study can be used effectively to guide treatment procedures.

Acknowledgment

This work was supported in part by a grant from the College of Graduate Studies and Research of the University of Central Oklahoma and by a grant from the National Institute of Health (P20 RR016478 from the Ideal Networks for Biomedical Research Excellence (INBRE) Program of the National Center for Research Resources).

References

1. W. R. Chen, R. L. Adams, S. Heaton, D. T. Dickey, K. E. Bartels, and R. E. Nordquist, "Chromophore-enhanced laser-tumor tissue photothermal interactions using 808 nm diode laser," *Cancer Lett.* **88**, 15–19 (1995).
2. W. R. Chen, R. L. Adams, K. E. Bartels, and R. E. Nordquist,

- “Chromophore-enhanced in vivo tumor cell destruction using 808 nm diode laser,” *Cancer Lett.* **94**, 125–131 (1995).
3. W. R. Chen, R. L. Adams, A. K. Higgins, K. E. Bartels, and R. E. Nordquist, “Photo-thermal effects on murine mammary tumors using indocyanine green and 808 nm diode laser: an in vivo efficacy study,” *Cancer Lett.* **98**, 169–173 (1996).
4. L. R. Hirsch, R. J. Stafford, J. A. Bankson, S. R. Sershen, B. Rivera, R. E. Price, J. D. Hazle, N. J. Halas, and J. L. West, “Nanoshell-mediated near-infrared thermal therapy of tumors under magnetic resonance guidance,” *Proc. Natl. Acad. Sci. U.S.A.* **100**, 13549–13554 (2003).
5. L. J. Anghileri and J. Robort, *Hyperthermia in Cancer Treatment*, CRC Press, Boca Raton, FL (1986).
6. M. W. Dewhirst, W. G. Conner, and D. A. Sim, “Preliminary result of phase III trial of spontaneous animal tumors to heat and/ or radiation early normal tissue response and tumor volume influence on initial response,” *Int. J. Radiat. Oncol., Biol., Phys.* **8**, 1951–1962 (1982).
7. W. R. Chen, R. L. Adams, and R. E. Nordquist, “Laser-photosensitizer assisted immunotherapy: A novel modality in cancer treatment,” *Cancer Lett.* **115**, 25–30 (1997).
8. W. R. Chen, W. G. Zhu, J. R. Dynlacht, H. Liu, and R. E. Nordquist, “Long-term tumor resistance induced by laser photo-immunotherapy,” *Int. J. Cancer* **81**, 808–812 (1999).
9. L. Wang and S. Jacques, *Monte Carlo Modeling of Light Transport in Multi-layered Tissues in Standard C*, Plenum Press, New York (1998).
10. L. H. Wang, R. E. Nordquist, and W. R. Chen, “Optimal beam size for light delivery to absorption-enhanced tumors buried in biological tissues and effect of multiple beam delivery: a Monte Carlo study,” *Appl. Opt.* **36**, 8286–8291 (1997).
11. L. Wang and S. Jacques, “Monte Carlo modeling of light transport in multi-layered tissues,” Laser Biology Research Lab., The Univ. Texas M.D. Anderson Cancer Center (1995); <http://oilab.tamu.edu/mcr5/Mcman.pdf>
12. L. G. Henyey and J. L. Greenstein, “Diffuse radiation in the galaxy,” *Astrophys. J.* **93**, 70–83 (1941).
13. B. Carnahan, *Applied Numerical Methods*, John Wiley and Sons, New York (1969).
14. S. Chapra, *Numerical Methods for Engineers*, McGraw-Hill Book Company, New York (1988).
15. J. Lienhard, IV and J. Lienhard V, *A Heat Transfer Textbook*, Phlogiston Press, Lexington, MA (2002).